

# MYP Mathematics

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A companion manual to support  
*Principles to Practice* and the *Subject Guide*

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# Table of Contents

<b>Conceptual Understanding</b>	<b>2</b>
Key Concepts	2
Related Concepts	4
Global Contexts	5
<b>Teaching and Learning Through Inquiry</b>	<b>7</b>
Statements of Inquiry	7
Inquiry Questions	7
Examples	7
<b>Mathematics Learning Objectives</b>	<b>9</b>
Objective A: Knowing and Understanding	10
Objective B: Investigating Patterns	11
Objective C: Communicating	12
Objective D: Applying Math in Real Life Contexts	13
<b>Assessment in the MYP</b>	<b>14</b>
Assessment Practices	14
Assessment Tasks in MYP Math	15
Task Specific Rubrics	16
Achievement Levels and Assigning Grades	17
Measuring Student Growth	17
<b>Approaches to Learning Skills</b>	<b>18</b>
<b>Unit Planner Guide</b>	<b>23</b>

# Conceptual Understanding

A concept is a “big idea”—a principle or notion that is enduring, the significance of which goes beyond particular origins, subject matter or a place in time. Concepts represent the vehicle for students’ inquiry into the issues and ideas of personal, local and global significance, providing the means by which they can explore the essence of mathematics.

Concepts have an important place in the structure of knowledge that requires students and teachers to think with increasing complexity as they organize and relate facts and topics. Concepts express understanding that students take with them into lifelong adventures of learning. They help students to develop principles, generalizations and theories. Students use conceptual understanding as they solve problems, analyse issues and evaluate decisions that can have an impact on themselves, their communities and the wider world.

In the MYP, conceptual understanding is framed by prescribed key and related concepts. Teachers must use these concepts to develop the curriculum

## KEY CONCEPTS

Key concepts promote interdisciplinary understanding. They represent big ideas that are both within and across disciplines and subjects.

The MYP has chosen 16 key concepts to be explored across all subjects, but 4 have been identified as the framework for mathematics. As your focus for the year, these concepts will inform units of work and help to organize teaching and learning. Unit of study will focus on one to two key concepts and each concept should be addressed at least once in the duration of the course.

Aesthetics	Change	Communication	Communities
Connections	Creativity	Culture	Development
<b>Form</b>	Global Interactions	Identity	<b>Logic</b>
Perspective	<b>Relationships</b>	Systems	Time, Place, & Space

## Form

**Form** is the shape and underlying structure of an entity or piece of work, including its organization, essential nature and external appearance.

Form in MYP mathematics refers to the understanding that the underlying structure and shape of an entity is distinguished by its properties. Form provides opportunities for students to appreciate the aesthetic nature of the constructs used in a discipline.

## **Logic**

**Logic** is a method of reasoning and a system of principles used to build arguments and reach conclusions.

Logic in MYP mathematics is used as a process in making decisions about numbers, shapes, and variables. This system of reasoning provides students with a method for explaining the validity of their conclusions. Within the MYP, this should not be confused with the subfield of mathematics called “symbolic logic”.

## **Relationships**

**Relationships** allow students to identify and understand connections and associations between properties, objects, people and ideas—including the human community’s connections with the world in which we live. Any change in relationships brings consequences—some of which may occur on a small scale, while others may be far-reaching, affecting large systems like human societies and the planet as a whole.

Relationships in MYP mathematics refers to the connections between quantities, properties or concepts and these connections may be expressed as models, rules or statements. Relationships provide opportunities for students to explore patterns in the world around them. Connections between the student and mathematics in the real world are important in developing deeper understanding.

## RELATED CONCEPTS

Related concepts promote deep learning. They are grounded in specific disciplines and are useful for exploring key concepts in greater detail. Inquiry into related concepts helps students develop more complex and sophisticated conceptual understanding. Related concepts may arise from the subject matter of a unit or the craft of a subject—its features and processes.

Change	A variation in size, amount or behaviour
Equivalence	The state of being identically equal or interchangeable, applied to statements, quantities, or expressions
Generalization	A general statement made on the basis of specific examples
Justification	Valid reasons or evidence used to support a statement
Measurement	A method of determining quantity, capacity or dimension using a defined Unit
Model	A depiction of a real-life event using expressions, equations or graphs
Pattern	A set of numbers or objects that follow a specific order or rule
Quality	An amount or number
Representation	The manner in which something is presented
Simplification	The process of reducing to a less complicated form
Space	The frame of geometrical dimensions describing an entity
System	Valid reasons or evidence used to support a statement

## Global Contexts

Global contexts direct learning towards independent and shared inquiry into our common humanity and shared guardianship of the planet. Using the world as the broadest context for learning, MYP mathematics can develop meaningful explorations. Many inquiries into mathematics concepts naturally focus on scientific and technical innovation. However, courses in this subject group should, over time, offer students multiple opportunities to explore all MYP global contexts in relationship to the aims and objectives of the subject group.

## MYP Global Contexts

<p style="text-align: center;"><b>identities and relationships</b></p> <p style="text-align: center;"><i>Who am I? Who are we?</i></p>	<p>Students will explore identity; beliefs and values; personal, physical, mental, social and spiritual health; human relationships including families, friends, communities and cultures; what it means to be human.</p>	<p>Possible explorations to develop:</p> <ul style="list-style-type: none"> <li>• competition and cooperation; teams, affiliation and leadership</li> <li>• identity formation, self-esteem, status, roles and role models</li> <li>• personal efficacy and agency; attitudes, motivations, independence; happiness and the good life</li> <li>• physical, psychological and social development, transitions, health and well-being, lifestyle choices</li> <li>• human nature and human dignity, moral reasoning and ethical judgment, consciousness and mind</li> </ul>
<p style="text-align: center;"><b>orientation in time and space</b></p> <p style="text-align: center;"><i>What is the meaning of 'where' and 'when'?</i></p>	<p>Students will explore personal histories; homes and journeys; turning points in humankind; discoveries; explorations and migrations of humankind; the relationships between, and the interconnectedness of, individuals and civilizations, from personal, local and global perspectives.</p>	<p>Possible explorations to develop:</p> <ul style="list-style-type: none"> <li>• civilizations and social histories, heritage; pilgrimage, migration, displacement and exchange</li> <li>• epochs, eras, turning points and 'big history'</li> <li>• scale, duration, frequency and variability</li> <li>• peoples, boundaries, exchange and interaction</li> <li>• natural and human landscapes and resources</li> <li>• evolution, constraints and adaptation</li> </ul>
<p style="text-align: center;"><b>personal and cultural expression</b></p> <p style="text-align: center;"><i>What is the nature and purpose of creative expression?</i></p>	<p>Students will explore the ways in which we discover and express ideas, feelings, nature, culture, beliefs and values; the ways in which we reflect on, extend and enjoy our creativity; our appreciation of the aesthetic.</p>	<p>Possible explorations to develop:</p> <ul style="list-style-type: none"> <li>• artistry, craft, creation, beauty</li> <li>• products, systems and institutions</li> <li>• social constructions of reality; philosophies and ways of life; belief systems; ritual and play</li> <li>• critical literacy, languages and linguistic systems; histories of ideas, fields and disciplines; analysis and argument</li> <li>• metacognition and abstract thinking</li> <li>• entrepreneurship, practice and competency</li> </ul>

## MYP Global Contexts

<p><b>scientific and technical innovation</b></p> <p><i>How do we understand the worlds in which we live?</i></p>	<p>Students will explore the natural world and its laws; the interaction between people and the natural world; how humans use their understanding of scientific principles; the impact of scientific and technological advances on communities and environments; the impact of environments on human activity; how humans adapt environments to their needs.</p>	<p>Possible explorations to develop:</p> <ul style="list-style-type: none"> <li>• systems, models, methods; products, processes and solutions</li> <li>• adaptation, ingenuity and progress</li> <li>• opportunity, risk, consequences and responsibility</li> <li>• modernization, industrialization and engineering</li> <li>• digital life, virtual environments and the information age</li> <li>• the biological revolution</li> <li>• mathematical puzzles, principles and discoveries</li> </ul>
<p><b>globalization and sustainability</b></p> <p><i>How is everything connected?</i></p>	<p>Students will explore the interconnectedness of human-made systems and communities; the relationship between local and global processes; how local experiences mediate the global; reflect on the opportunities and tensions provided by world-interconnectedness; the impact of decision-making on humankind and the environment.</p>	<p>Possible explorations to develop:</p> <ul style="list-style-type: none"> <li>• markets, commodities and commercialization</li> <li>• human impact on the environment</li> <li>• commonality, diversity and interconnection</li> <li>• consumption, conservation, natural resources and public goods</li> <li>• population and demography</li> <li>• urban planning, strategy and infrastructure</li> </ul>
<p><b>fairness and development</b></p> <p><i>What are the consequences of our common humanity?</i></p>	<p>Students will explore rights and responsibilities; the relationship between communities; sharing finite resources with other people and with other living things; access to equal opportunities; peace and conflict resolution.</p>	<p>Possible explorations to develop:</p> <ul style="list-style-type: none"> <li>• democracy, politics, government and civil society</li> <li>• inequality, difference and inclusion</li> <li>• human capability and development ; social entrepreneurs</li> <li>• rights, law, civic responsibility and the public sphere</li> <li>• justice, peace and conflict management</li> <li>• power and privilege</li> <li>• authority , security and freedom</li> <li>• imagining a hopeful future</li> </ul>

# Teaching and Learning Through Inquiry

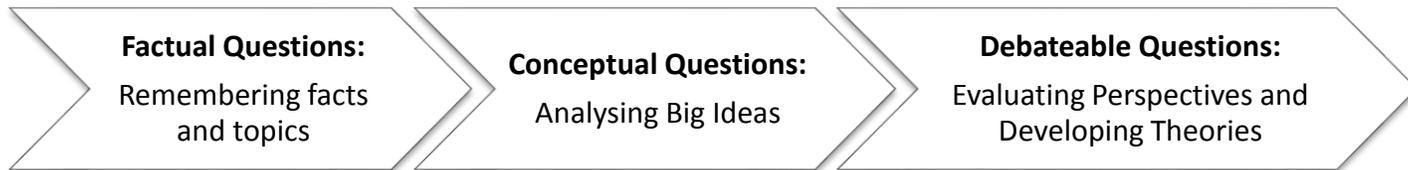
## Statements of Inquiry

A statement of inquiry sets conceptual understanding in a global context in order to frame classroom inquiry and direct purposeful learning

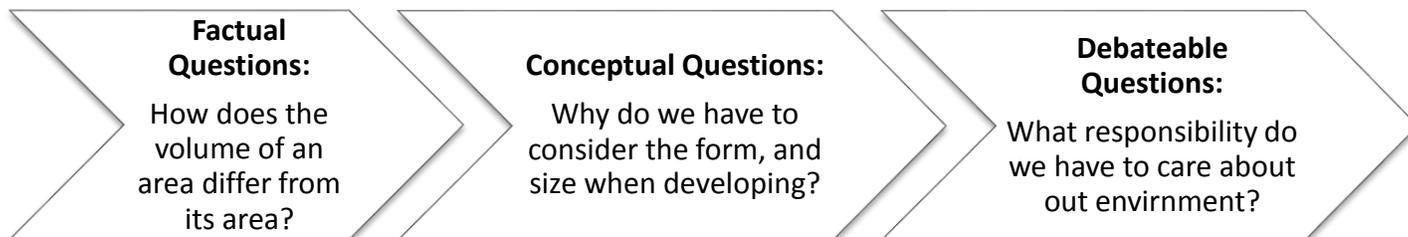
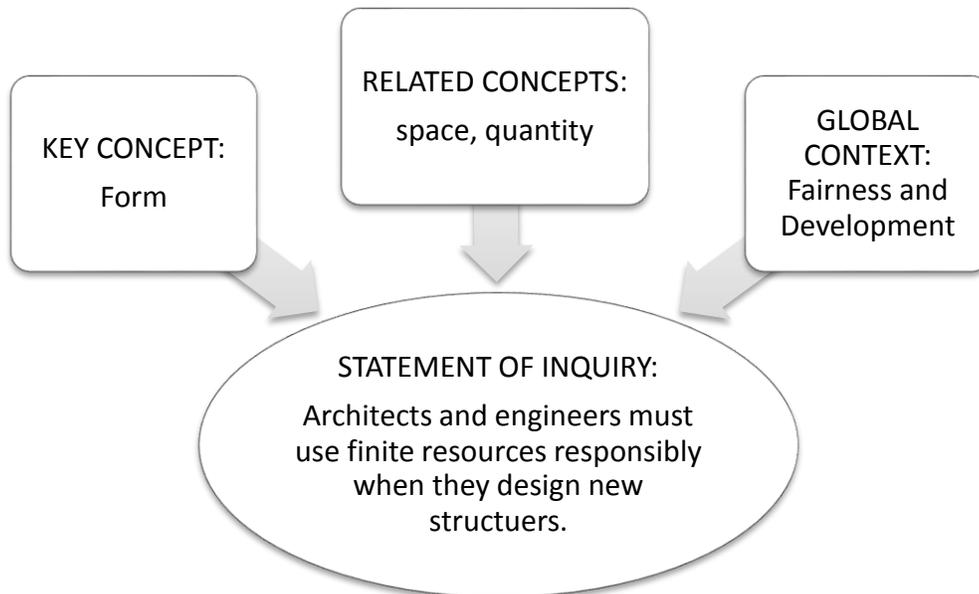


## Inquiry Questions

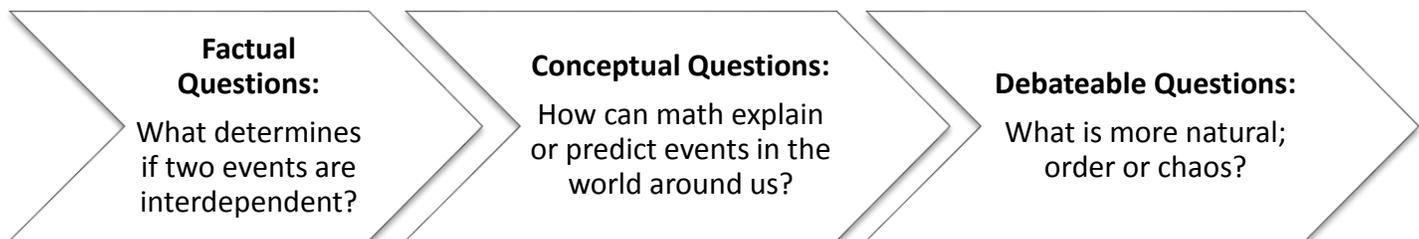
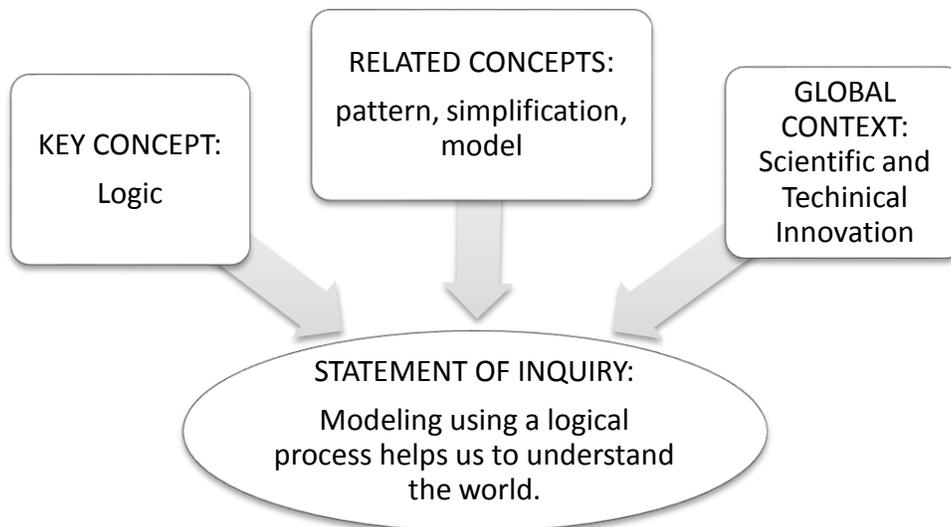
Teachers and students use statements of inquiry to help them identify factual, conceptual and debatable inquiry questions. Inquiry questions give direction to teaching and learning, and they help to organize and sequence learning experiences.



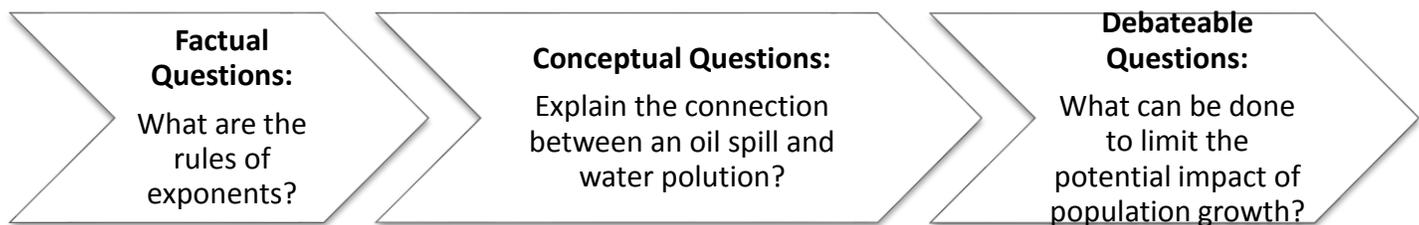
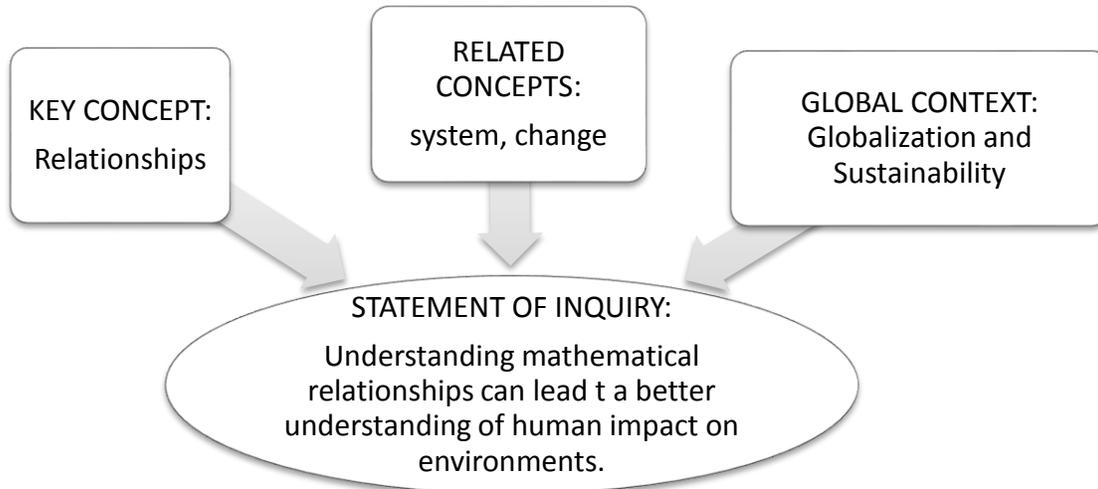
**Possible Project/Study:** Geometry and Trigonometry - volume



**Possible Project/Study:** Algebra – projectile motion



**Possible Project/Study:** Number – exponentials and logarithms



# Mathematics Learning Objectives

The objectives of any MYP subject state the specific targets that are set for learning in the subject. They define what the student will be able to accomplish as a result of studying the subject.

The objectives of MYP mathematics encompass the factual, conceptual, procedural and metacognitive dimensions of knowledge.

Each objective is elaborated by a number of **strands**; a strand is an aspect or indicator of the learning expectation.

Together these objectives reflect the knowledge, skills and attitudes that students need in order to use mathematics in a variety of contexts (including real-life situations), perform investigations and communicate mathematics clearly.

Subject groups **must** address all strands of **all** four objectives **at least twice** in each year of the MYP.

In order to keep track of the standards used in each unit and the number of times it has been used, teachers/PLTs may want to develop a system or check list. Below is an example.

OBJECTIVE	STRAND	UNIT WHERE IT IS ASSESSED		
Knowing and understanding	1			
	2			
	3			
	4			

## Objective A. Knowing and understanding

Knowledge and understanding are fundamental to studying mathematics and form the base from which to explore concepts and develop skills. This objective assesses the extent to which students can select and apply mathematics to solve problems in both familiar and unfamiliar situations in a variety of contexts.

This objective requires students to demonstrate knowledge and understanding of the concepts and skills of the four branches of mathematics (number, algebra, geometry and trigonometry, statistics and probability).

In order to reach the aims of mathematics, students should be able to:

- i. select appropriate mathematics when solving problems in both familiar and unfamiliar situations
- ii. apply the selected mathematics successfully when solving problems
- iii. solve problems correctly in a variety of contexts.

Achvmt Level	Level Descriptor
0	The student <b>does not</b> reach a standard described by any of the descriptors below.
1-2	The student is able to: i. <b>select</b> appropriate mathematics when solving simple problems in familiar situations ii. <b>apply</b> the selected mathematics successfully when solving these problems iii. generally <b>solve</b> these problems correctly
3-4	The student is able to: i. <b>select</b> appropriate mathematics when solving more complex problems in familiar situations ii. <b>apply</b> the selected mathematics successfully when solving these problems iii. generally <b>solve</b> these problems correctly
5-6	The student is able to: i. <b>select</b> appropriate mathematics when solving challenging problems in familiar situations ii. <b>apply</b> the selected mathematics successfully when solving these problems iii. generally <b>solve</b> these problems correctly.
7-8	The student is able to: i. <b>select</b> appropriate mathematics when solving challenging problems in both familiar and unfamiliar situations ii. <b>apply</b> the selected mathematics successfully when solving these problems iii. generally <b>solve</b> these problems correctly

## Objective B. Investigating patterns

Investigating patterns allows students to experience the excitement and satisfaction of mathematical discovery. Working through investigations encourages students to become risk-takers, inquirers and critical thinkers. The ability to inquire is invaluable in the MYP and contributes to lifelong learning.

In order to reach the aims of mathematics, students should be able to:

- i. select and apply mathematical problem-solving techniques to discover complex patterns
- ii. describe patterns as general rules consistent with findings
- iii. prove, or verify and justify, general rules.

Achvmt Level	Level Descriptor
0	The student <b>does not</b> reach a standard described by any of the descriptors below.
1-2	The student is able to: i. <b>apply</b> , with teacher support, mathematical problem-solving techniques to discover simple patterns ii. <b>state</b> predictions consistent with patterns.
3-4	The student is able to: i. <b>apply</b> mathematical problem-solving techniques to discover simple patterns ii. <b>suggest</b> general rules consistent with findings
5-6	The student is able to: i. <b>select</b> and <b>apply</b> mathematical problem-solving techniques to discover complex patterns ii. <b>describe</b> patterns as general rules consistent with findings iii. <b>verify</b> the validity of these general rules.
7-8	The student is able to: i. <b>select</b> and <b>apply</b> mathematical problem-solving techniques to discover complex patterns ii. <b>describe</b> patterns as general rules consistent with correct findings iii. <b>prove</b> , or <b>verify</b> and <b>justify</b> , these general rules.

## Objective C: Communicating

Mathematics provides a powerful and universal language. Students are expected to use appropriate mathematical language and different forms of representation when communicating mathematical ideas, reasoning and findings, both orally and in writing.

In order to reach the aims of mathematics, students should be able to:

- i. use appropriate mathematical language (notation, symbols and terminology) in both oral and written explanations
- ii. use appropriate forms of mathematical representation to present information
- iii. move between different forms of mathematical representation
- iv. communicate complete, coherent and concise mathematical lines of reasoning
- v. organize information using a logical structure.

Achvmt Level	Level Descriptor
0	The student <b>does not</b> reach a standard described by any of the descriptors below.
1-2	The student is able to: i. <b>use</b> limited mathematical language ii. <b>use</b> limited forms of mathematical representation to present information iii. <b>communicate</b> through lines of reasoning that are difficult to interpret.
3-4	The student is able to: i. <b>use</b> some appropriate mathematical language ii. <b>use</b> appropriate forms of mathematical representation to present information adequately iii. <b>communicate</b> through lines of reasoning that are complete iv. adequately <b>organize</b> information using a logical structure.
5-6	The student is able to: i. usually <b>use</b> appropriate mathematical language ii. usually <b>use</b> appropriate forms of mathematical representation to present information correctly iii. usually move between different forms of mathematical representation iv. <b>communicate</b> through lines of reasoning that are complete and coherent v. <b>present</b> work that is usually organized using a logical structure.
7-8	The student is able to: i. consistently <b>use</b> appropriate mathematical language ii. <b>use</b> appropriate forms of mathematical representation to consistently present information correctly iii. move effectively between different forms of mathematical representation iv. <b>communicate</b> through lines of reasoning that are complete, coherent and concise v. <b>present</b> work that is consistently organized using a logical structure

## Objective D: Using language

MYP mathematics encourages students to see mathematics as a tool for solving problems in an authentic real-life context. Students are expected to transfer theoretical mathematical knowledge into real-world situations and apply appropriate problem-solving strategies, draw valid conclusions and reflect upon their results.

In order to reach the aims of mathematics, students should be able to:

- i. identify relevant elements of authentic real-life situations
- ii. select appropriate mathematical strategies when solving authentic real-life situations
- iii. apply the selected mathematical strategies successfully to reach a solution
- iv. justify the degree of accuracy of a solution
- v. justify whether a solution makes sense in the context of the authentic real-life situation.

Achvmnt Level	Level Descriptor
0	The student <b>does not</b> reach a standard described by any of the descriptors below.
1-2	The student is able to: i. <b>identify</b> some of relevant elements of the authentic real-life situation ii. <b>apply</b> mathematical strategies to reach a correct solution to the authentic real-life situation, with limited success
3-4	The student is able to: i. <b>identify</b> the relevant elements of the authentic real-life situation ii. <b>select</b> , with some success, adequate mathematical strategies to model the authentic real-life situation iii. <b>apply</b> mathematical strategies to reach a correct solution to the authentic real-life situation iv. <b>discuss</b> whether the solution makes sense in the context of the authentic real-life situation.
5-6	The student is able to: i. <b>identify</b> the relevant elements of the authentic real-life situation ii. <b>select</b> adequate mathematical strategies to model the authentic real-life situation iii. <b>apply</b> the selected mathematical strategies to reach a valid solution to the authentic real-life situation iv. <b>explain</b> the degree of accuracy of the solution v. <b>explain</b> whether the solution makes sense in the context of the authentic real-life situation.
7-8	The student is able to: i. <b>identify</b> the relevant elements of the authentic real-life situation ii. <b>select</b> appropriate mathematical strategies to model the authentic real-life situation iii. <b>apply</b> the selected mathematical strategies to reach a correct solution to the authentic real-life situation iv. <b>justify</b> the degree of accuracy of the solution v. <b>justify</b> whether the solution makes sense in the context of the authentic real-life situation.

# Assessment in the MYP

Assessment practices in the MYP aim to

- support student learning by providing consistent feedback on the learning process
- provide opportunities for students to demonstrate transfer of skills across disciplines
- develop critical and creative thinking skills
- assign the most accurate achievement level for student performance, rather than averaging achievement levels over a given period of time
- assess student understanding at the end of a course

Choosing from a range of **assessment strategies**, teachers can devise **assessment tasks** that give students opportunities to show clearly what they can achieve in relation to the Statement of Inquiry, the MYP objectives, and state standards of the unit. Teachers will ensure that they document and record student performance using various **assessment tools**.

ASSESSMENT STRATEGIES	ASSESSMENT TASKS	ASSESSMENT TOOLS
<p><b>Observation</b> Whole class or individual; as a non-participant or while engaged</p> <p><b>Selected Response</b> Asking specific or general questions to elicit responses from students</p> <p><b>Open Ended Tasks</b> Provide students with a stimulus and ask students to provide an original response – presentations, diagrams</p> <p><b>Performance</b> Allow students to show that they can do something with the knowledge that they have gained</p> <p><b>Process Journals</b> Encourages reflection and metacognition in students; allows for communication between student and teacher</p> <p><b>Portfolio Assessment</b> Collection of work that shows student mastery of content</p>	<p><b>Composition</b> Musical, physical, or artistic</p> <p><b>Creations of Solutions</b> In response to given problems</p> <p><b>Essays</b></p> <p><b>Examinations</b></p> <p><b>Questionnaires</b></p> <p><b>Investigations</b></p> <p><b>Research</b></p> <p><b>Presentations</b> Verbal (oral or written) or graphic; uses various media</p>	<p><b>Anecdotal Records</b> Brief written notes regarding whole class or individual performance</p> <p><b>Continuums</b> Visual representation of students development that helps identify next stages of learning</p> <p><b>Rubrics</b> Measure students' performance at a variety of levels</p> <p><b>Examples</b> Using student work as concrete examples of performance at various achievement levels</p> <p><b>Checklists</b> Check off when students demonstrate a particular response to a task</p>

## Assessment Tasks in MYP Mathematics

Criterion	Typical Assessment Tasks	Notes
Criterion A (knowing and understanding)	Classroom tests Examinations Assignments that include both familiar and unfamiliar situations	Teachers who choose to use criterion A with criterion B should be able to clearly define which aspects of the task will be assessed with each criterion, ensuring that the task is rigorous enough to allow students to achieve the highest levels of both criteria.
Criterion B (investigating practices)	Mathematical investigations of some complexity that allow students: <ul style="list-style-type: none"> <li>• to choose their own mathematical techniques</li> <li>• to reason from the specific to the general</li> </ul>	Assessment tasks could have a variety of solutions and should enhance independent mathematical thinking.
Criterion C (communicating)	Investigations and real-life problems Reports that: <ul style="list-style-type: none"> <li>• require logical structure</li> <li>• allow multiple forms of representation to present information</li> </ul>	Tests are not appropriate to assess this criterion since there is no logical structure to the whole piece of work that is submitted by the student. Criterion C is used when students present a report, for example, that requires a logical structure in order to be followed and that would allow for several forms of representation to be used to present information.
Criterion D (applying mathematics in real-life contexts)	Opportunities to use mathematical concepts to solve real-life problems	For example: modelling or curve-fitting tasks based in authentic contexts. Mathematics can be used to model many situations (for example, painting room, analysing mobile telephone tariff plans, triangulation, diet plans).

## Developing Task Specific Rubrics

### WHY?

1. Brings transparency to the assessment process for students, teachers, parents
2. Provides clear measurable evidence of learning
3. Can be used year after year
4. Can be modified as the units are revised
5. Contribute to the teacher reflections of units

### HOW?

1. Study the assessment criteria; these are very vague and generalized
2. Study your assessment task
3. Redraft the level descriptors to match your specific assessment task for the unit

### THINGS TO CONSIDER

1. When sharing the rubrics with students, make sure they are written in student-friendly language. Rubrics must be written so that students understand them.
2. Students should be able to accomplish the highest level of achievement. Be careful not to design assessment tasks that are impossible for students.
3. The rubrics should be standardized across the course. Teachers and students should see consistency across every section of the course.

### RUBRIC EXAMPLES

This example is a selection used for a summative assessment for a probability unit using Criterion D.

Level	Level Descriptor	Task Specific Clarification
0	The student does not match any of the descriptors below.	You did not reach a standard as described by any of the descriptors below.
1-2	The student is able to: i. <b>identify</b> some of relevant elements of the authentic real-life situation ii. <b>apply</b> mathematical strategies to reach a correct solution to the authentic real-life situation, with limited success	You demonstrated the ability to: - identify the probability of S or U and the types of game playing events to which these relate. - attempt to obtain a solution and a set on conclusions about your success in continuing to attempt the game.
3-4	The student is able to: i. <b>identify</b> the relevant elements of the authentic real-life situation ii. <b>select</b> , with some success, adequate mathematical strategies to model the authentic real-life situation iii. <b>apply</b> mathematical strategies to reach a correct solution to the authentic real-life situation iv. <b>discuss</b> whether the solution makes sense in the context of the authentic real-life situation.	You demonstrated the ability to: - identify the probability of U and S and the types of game playing events to which these relate. - select some adequate strategies needed to model the probability of success and failure when continuing to attempt the game - apply strategies to obtain a solution set of conclusions about your success in continuing to attempt the game - discuss you conclusions in the context of real life attempts at success by continuing to play the game.

## Achievement Levels and Assigning Grades

Each criterion is divided into various achievement levels. The level descriptors for each band describe a range of student performance in the various strands of each objective. At the lowest levels, student achievement in each of the strands will be minimal. As the numerical levels increase, the level descriptors describe greater achievement levels in each of the strands.

When applying the assessment criteria to student performance, the teacher should determine whether the first descriptor describes the performance. If the student work exceeds the expectations of the first descriptor, the teacher should determine whether it is described by the second descriptor. This should continue until the teacher arrives at a descriptor that does not describe the student work; the work will then be described by the previous descriptor. In certain cases, it may appear that the student has not fulfilled all of the descriptors in a lower band but has fulfilled some in a higher band. In those cases, teachers must use their professional judgment in determining the descriptor that best fits the student's performance.

## Measuring Student Growth throughout the Course

MYP assessment focuses on student understanding at the end of the course but also requires teachers to determine the most accurate demonstration of student understanding. This means recording and tracking student performance on each criterion as it is assessed for the duration of the course. Remember, subject areas must address all strands of all four assessment criteria at least twice each year. This allows students and teachers to measure growth over time.

An example of one monitoring system is shown below. In this model, teachers can include students in the process by asking them to maintain the record of achievement and allow time for reflection on performance.

Criterion	Unit	Task	Grade

# Approaches to Learning Skills

Through approaches to learning (ATL) in IB programmes, students develop skills that have relevance across the curriculum that help them “learn how to learn”. ATL skills can be learned and taught, improved with practice and developed incrementally. They provide a solid foundation for learning independently and with others. ATL skills help students prepare for, and demonstrate learning through, meaningful assessment. They provide a common language that students and teachers can use to reflect on, and articulate on, the process of learning. All MYP teachers are responsible for integrating and explicitly teaching ATL skills.

Well-designed learning engagements and assessments provide rich opportunities for students to practise and demonstrate ATL skills. Each MYP unit explicitly identifies ATL skills around which teaching and learning can focus and through which students can authentically demonstrate what they are able to do. Formative assessments provide important feedback for developing discrete skills, and many ATL skills support students as they demonstrate their achievements in summative assessments of subject group objectives.

## ATL Skills Important to Mathematics

Category	Skill indicator
Thinking skills	Use prioritization and order of precedence in problem-solving
Social skills	Help others to create success for themselves during group work
Communication skills	Organize and interpret data using both analogue and digital tools
Self-management skills	Practise focus and concentration while solving multiple problems
Research skills	Use a variety of technologies and media platforms, including social media and online networks, to source information

## ATL Skills Demonstrated in Mathematics

Approaches to learning
<p><b>Thinking (critical thinking):</b> draw justifiable conclusions and generalizations from investigating patterns</p> <p><b>Communication (reflection):</b> keep a regular journal during the investigation to maintain a record of reflections</p>

Category	Cluster	Skills
Research	Information Literacy Skills	<p><b>Finding, interpreting, judging and creating information</b></p> <ul style="list-style-type: none"> <li>• Collect, record and verify data</li> <li>• Access information to be informed and inform others</li> <li>• Make connections between various sources of information</li> <li>• Understand the benefits and limitations of personal sensory learning preferences when accessing, processing and recalling information</li> <li>• Use memory techniques to develop long-term memory</li> <li>• Present information in a variety of formats and platforms</li> <li>• Collect and analyse data to identify solutions and make informed decisions</li> <li>• Process data and report results</li> <li>• Evaluate and select information sources and digital tools based on their appropriateness to specific tasks</li> <li>• Understand and use technology systems</li> <li>• Use critical-literacy skills to analyse and interpret media communications</li> <li>• Understand and implement intellectual property rights</li> <li>• Create references and citations, use footnotes/endnotes and construct a bibliography according to recognized conventions</li> <li>• Identify primary and secondary sources</li> </ul>
	Media Literacy Skills	<p><b>Interacting with media to use and create ideas and information</b></p> <ul style="list-style-type: none"> <li>• Locate, organize, analyse, evaluate, synthesize and ethically use information from a variety of sources and media (including digital social media and online networks)</li> <li>• Demonstrate awareness of media interpretations of events and ideas (including digital social media)</li> <li>• Make informed choices about personal viewing experiences</li> <li>• Understand the impact of media representations and modes of presentation</li> <li>• Seek a range of perspectives from multiple and varied sources</li> <li>• Communicate information and ideas effectively to multiple audiences using a variety of media and formats</li> <li>• Compare, contrast and draw connections among (multi)media resources</li> </ul>

Category	Cluster	Skills
Communication	Communication Skills	<p><b>Exchanging thoughts, messages and information effectively through interaction</b></p> <ul style="list-style-type: none"> <li>• Give and receive meaningful feedback</li> <li>• Use intercultural understanding to interpret communication</li> <li>• Use a variety of speaking techniques to communicate with a variety of audiences</li> <li>• Use appropriate forms of writing for different purposes and audiences</li> <li>• Use a variety of media to communicate with a range of audiences</li> <li>• Interpret and use effectively modes of non-verbal communication</li> <li>• Negotiate ideas and knowledge with peers and teachers</li> <li>• Participate in, and contribute to, digital social media networks</li> <li>• Collaborate with peers and experts using a variety of digital environments and media</li> <li>• Share ideas with multiple audiences using a variety of digital environments and media</li> </ul>
		<p><b>Reading, writing and using language to gather and communicate information</b></p> <ul style="list-style-type: none"> <li>• Read critically and for comprehension</li> <li>• Read a variety of sources for information and for pleasure</li> <li>• Make inferences and draw conclusions</li> <li>• Use and interpret a range of discipline-specific terms and symbols</li> <li>• Write for different purposes</li> <li>• Understand and use mathematical notation</li> <li>• Paraphrase accurately and concisely</li> <li>• Preview and skim texts to build understanding</li> <li>• Take effective notes in class</li> <li>• Make effective summary notes for studying</li> <li>• Use a variety of organizers for academic writing tasks</li> <li>• Find information for disciplinary and interdisciplinary inquiries, using a variety of media</li> <li>• Organize and depict information logically</li> <li>• Structure information in summaries, essays and reports</li> </ul>
Social	Collaboration Skills	<p><b>Working effectively with others</b></p> <ul style="list-style-type: none"> <li>• Use social media networks appropriately to build and develop relationships</li> <li>• Practise empathy</li> <li>• Delegate and share responsibility for decision-making</li> <li>• Help others to succeed</li> <li>• Take responsibility for one's own actions</li> <li>• Manage and resolve conflict, and work collaboratively in teams</li> <li>• Build consensus</li> <li>• Make fair and equitable decisions</li> <li>• Listen actively to other perspectives and ideas</li> <li>• Negotiate effectively</li> <li>• Encourage others to contribute</li> <li>• Exercise leadership and take on a variety of roles within groups</li> <li>• Give and receive meaningful feedback</li> <li>• Advocate for one's own rights and needs</li> </ul>

Category	Cluster	Skills
Self-Management	Organization Skills	<p><b>Managing time and tasks effectively</b></p> <ul style="list-style-type: none"> <li>• Plan short- and long-term assignments; meet deadlines</li> <li>• Create plans to prepare for summative assessments (examinations and performances)</li> <li>• Keep and use a weekly planner for assignments</li> <li>• Set goals that are challenging and realistic</li> <li>• Plan strategies and take action to achieve personal and academic goals</li> <li>• Bring necessary equipment and supplies to class</li> <li>• Keep an organized and logical system of information files/notebooks</li> <li>• Use appropriate strategies for organizing complex information</li> <li>• Understand and use sensory learning preferences (learning styles)</li> <li>• Select and use technology effectively and productively</li> </ul>
	Affective Skills	<p><b>Managing state of mind</b></p> <ul style="list-style-type: none"> <li>• Mindfulness <ul style="list-style-type: none"> <li>– Practise focus and concentration</li> <li>– Practise strategies to develop mental focus</li> <li>– Practise strategies to overcome distractions</li> </ul> </li> <li>• Perseverance <ul style="list-style-type: none"> <li>– Demonstrate persistence and perseverance</li> <li>– Practise delaying gratification</li> </ul> </li> <li>• Emotional management <ul style="list-style-type: none"> <li>– Practise strategies to overcome impulsiveness and anger</li> <li>– Practise strategies to prevent and eliminate bullying</li> <li>– Practise strategies to reduce stress and anxiety</li> </ul> </li> <li>• Self-motivation <ul style="list-style-type: none"> <li>– Practise analysing and attributing causes for failure</li> <li>– Practise managing self-talk</li> <li>– Practise positive thinking</li> </ul> </li> <li>• Resilience <ul style="list-style-type: none"> <li>– Practise “bouncing back” after adversity, mistakes and failures</li> <li>– Practise dealing with disappointment and unmet expectations</li> <li>– Practise dealing with change</li> </ul> </li> </ul>
	Reflection Skills	<p><b>(Re)considering the process of learning; choosing and using ATL skills</b></p> <ul style="list-style-type: none"> <li>• Develop new skills, techniques and strategies for effective learning</li> <li>• Identify strengths and weaknesses of personal learning strategies</li> <li>• Demonstrate flexibility in the selection and use of learning strategies</li> <li>• Consider content (What did I learn about today? What don't I yet understand? What questions do I have now?)</li> <li>• Consider ATL skills development (What can I already do? How can I share my skills to help peers who need more practice? What will I work on next?)</li> <li>• Consider personal learning strategies (What can I do to become a more efficient and effective learner? How can I become more flexible in my choice of learning strategies? What factors are important for helping me learn well?)</li> <li>• Focus on the process of creating by imitating the work of others</li> <li>• Consider ethical, cultural and environmental implications</li> <li>• Keep a journal to record reflections</li> </ul>

Category	Cluster	Skills
Thinking	Critical Thinking Skills	<p><b>Analysing and evaluating issues and ideas</b></p> <ul style="list-style-type: none"> <li>• Practise observing carefully in order to recognize problems</li> <li>• Gather and organize relevant information to formulate an argument</li> <li>• Recognize unstated assumptions and bias</li> <li>• Interpret data</li> <li>• Evaluate evidence and arguments</li> <li>• Recognize and evaluate propositions</li> <li>• Draw reasonable conclusions and generalizations</li> <li>• Test generalizations and conclusions</li> <li>• Revise understanding based on new information and evidence</li> <li>• Evaluate and manage risk</li> <li>• Formulate factual, topical, conceptual and debatable questions</li> <li>• Consider ideas from multiple perspectives</li> <li>• Develop contrary or opposing arguments</li> <li>• Analyse complex concepts and projects into their constituent parts and synthesize them to create new understanding</li> <li>• Propose and evaluate a variety of solutions</li> <li>• Identify obstacles and challenges</li> <li>• Use models and simulations to explore complex systems and issues</li> <li>• Identify trends and forecast possibilities</li> <li>• Troubleshoot systems and applications</li> </ul>
	Creative Thinking Skills	<p><b>Generating novel ideas and considering new perspectives</b></p> <ul style="list-style-type: none"> <li>• Use brainstorming and visual diagrams to generate new ideas and inquiries</li> <li>• Consider multiple alternatives, including those that might be unlikely or impossible</li> <li>• Create novel solutions to authentic problems</li> <li>• Make unexpected or unusual connections between objects and/or ideas</li> <li>• Design improvements to existing machines, media and technologies</li> <li>• Design new machines, media and technologies</li> <li>• Make guesses, ask “what if” questions and generate testable hypotheses</li> <li>• Apply existing knowledge to generate new ideas, products or processes</li> <li>• Create original works and ideas; use existing works and ideas in new ways</li> <li>• Practise flexible thinking—develop multiple opposing, contradictory and complementary arguments</li> <li>• Practise visible thinking strategies and techniques</li> <li>• Generate metaphors and analogies</li> </ul>
	Transfer Skills	<p><b>Using skills and knowledge in multiple contexts</b></p> <ul style="list-style-type: none"> <li>• Use effective learning strategies in subject groups and disciplines</li> <li>• Apply skills and knowledge in unfamiliar situations</li> <li>• Inquire in different contexts to gain a different perspective</li> <li>• Compare conceptual understanding across multiple subject groups and disciplines</li> <li>• Make connections between subject groups and disciplines</li> <li>• Combine knowledge, understanding and skills to create products or solutions</li> <li>• Transfer current knowledge to learning of new technologies</li> <li>• Change the context of an inquiry to gain different perspectives</li> </ul>

<b>Unit Title</b>	
<b>Course/Grade Level</b>	
<b>Teachers</b>	
<b>Length of Unit</b>	

### Stage 1 Integrate statement of inquiry, global context and inquiry questions

<b>Key Concept</b>	<b>Related Concepts</b>
Choose 1 (maybe 2) from the list	Choose 2 (maybe 3) from the list.

<b>Global Context</b>	Choose 1 from the list provided.
<b>Explanation for Global Context</b>	Include any bullet points from the list that students will explore in this unit.

<b>Statement of Inquiry</b>
A clear concise statement that includes the Key Concept and the Related Concept with regards to the Global Context.

<b>Inquiry Questions</b>	
<b>Factual</b>	Develop a question that rooted in the content, and is at the recall/remember level. Expect students to demonstrate understanding.
<b>Conceptual</b>	Develop a question that requires students to analyze the new knowledge in the context of the course.
<b>Debatable</b>	Develop a question that requires students to apply the new knowledge in a way that reaches beyond your course and connects the concept to other disciplines. This question should connect to your Statement of Inquiry.

**Assessment**

What task(s) will allow students the opportunity to respond to the unit question?

What will constitute acceptable evidence of understanding? How will students show what they have understood?

Each unit must include one summative assessment that will be graded on the IB subject specific criterion rubrics that are located in your subject guide.

If you are assigning a multiple choice test, it does not meet the assessment requirement unless it is graded with the IB rubrics.

If you assign multiple summative assessments, only include the assessment evaluated with the IB rubrics on the unit planner.

Briefly describe the assessment in this box.

Which specific MYP objectives will be addressed during this unit?

Copy and paste the MYP objectives from your subject guide.

Specific objectives should be chosen from the criterion. List the specific bullet points from those criteria that the unit will address. The bullets can come from multiple criteria.

Avoid saying "Criterion A" or "Investigate" because you may not be teaching every strand of that objective.

Which MYP assessment criteria will be used?

Identify the specific criterion rubric that will be used. This should be the Criterion that has the most bullet points listed above. Here you can say "Criterion A" or "Investigate".

**Stage 2 Backward planning: From the assessment to the learning activities through inquiry****Content**

What knowledge and/or skills (from the course overview) are going to be used to enable the student to respond to the unit question?

What (if any) state, provincial, district, or local standards/skills are to be addressed? How can they be unpacked to develop the significant concept(s) for stage 1?

You can list NCSCOS or Common Core Standards.

These can be copied and pasted.

<p><b>Learning experiences</b></p> <p>How will students know what is expected of them? Will they see examples, rubrics, templates?</p> <p>How will students acquire the knowledge and practise the skills required? How will they practise applying these?</p> <p>Do the students have enough prior knowledge? How will we know?</p>	<p><b>Teaching strategies</b></p> <p>How will we use formative assessment to give students feedback during the unit?</p> <p>What different teaching methodologies will we employ?</p> <p>How are we differentiating teaching and learning for all? How have we made provision for those learning in a language other than their mother tongue? How have we considered those with special educational needs?</p>
<p>Big Ideas to cover in these boxes:</p> <p>Differentiation strategies, literacy instruction, 21<sup>st</sup> century skill integration, technology integration.</p>	
<p>Just answer the questions above.</p>	<p>Just answer the questions above.</p>

Approaches to Learning		
Category	Cluster	Skill
<p>Identify the category, cluster and the specific skills you will teach. Can be bulleted list.</p>		
<p><b>Explanation of Instruction</b></p>	<p>Explain exactly how you will teach the skills you identified.</p>	

Learner Profile Traits Encouraged	Explanation of Inclusion
<p>Choose from the list.</p>	<p>Explain how this will be a part of the instruction.</p>

Opportunities for Volunteerism and Community Service
<p>Consider service opportunities, locally or globally, that connect with this topic. Could this unit develop into a service project for your students? How?</p>

## Resources

What resources are available to us?

How will our classroom environment, local environment and/or the community be used to facilitate students' experiences during the unit?

Be very specific when listing materials.

Imagine someone from another country reading your unit planner, how would they identify the resources that you have listed?

Include titles of books, textbooks, videos, etc.

## Ongoing reflections and evaluation

In keeping an ongoing record, consider the following questions.

### Students and teachers

What did we find compelling? Were our disciplinary knowledge/skills challenged in any way?

What inquiries arose during the learning? What, if any, extension activities arose?

How did we reflect—both on the unit and on our own learning?

### Possible connections

How successful was the collaboration with other teachers within my subject group and from other subject groups?

What interdisciplinary understandings were or could be forged through collaboration with other subjects?

### Assessment

Were students able to demonstrate their learning?

How did the assessment tasks allow students to demonstrate the learning objectives identified for this unit? How did I make sure students were invited to achieve at all levels of the criteria descriptors?

Are we prepared for the next stage?

### Data collection

How did we decide on the data to collect? Was it useful?

Include things to consider before the unit is taught.

What questions will students ask? What materials will I need? How can I incorporate other disciplines?

Include Post-teaching reflections. What went well? What can be improved?

As you reflect and revise unit planner, keep copies of the old unit planners as a way to measure growth and change.

IDEA-- Type each reflection in different color each year.

Then the file would only be saved once, but the reflections would be easy to identify each year.